

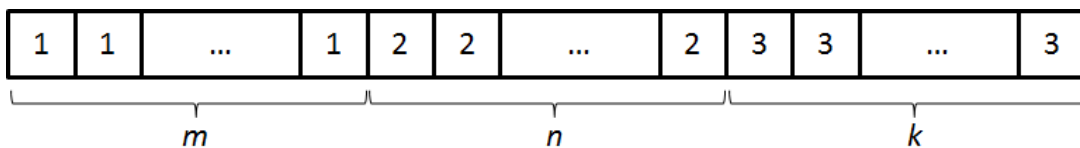
Bacterial population

Consider a population of bacteria, each with a certain type of plasmid: m with a plasmid type I, n with a plasmid type II and k with a plasmid type III. Every time two bacteria of a different plasmid type meet, their plasmid mutates to the subtraction of both types. For example, when a type I bacteria meets a type III bacteria, the plasmid mutates to a type II. Now we want to simulate the evolution of a given population throughout time.

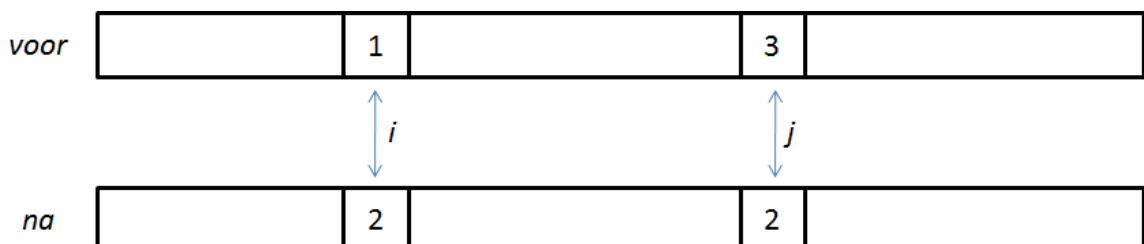
Assignment

Develop a class `Population` of which every object represents a population of bacterias. Each with a plasmid of a certain type. All objects must have an attribute `population`: a list of numbers with value 1, 2 or 3, where every element of the list represents a bacteria from the population and indicates the corresponding value of which type the bacteria has (at a certain point in time). Furthermore, all object must also have an attribute `encounters`, in which the number of encounters between bacteria is kept track of. The class `Population` must also support the following methods:

1. The initializing method `__init__` must make sure the attribute `population` represents an initial population with m bacteria with a plasmid type I, n with a plasmid type II and k with a plasmid type III. The values m , n and k are optional arguments of the method `__init__` with standard value 0. After executing this method, the attribute `encounters` of the new object must have value zero, and the attribute `population` must have a value as is shown in the scheme below.



2. The method `plasmids` must print a tuple (m, n, k) as a result, where the values m , n and k indicates the number of bacteria in the population with plasmids of respectively type I, type II and type III.
3. The method `__str__` must print a string of the format "type I : m , type II: n , type III: k (after x encounters)" as a result, where the values m , n , k and x must be filled out according to the current condition of the object.
4. The method `__repr__` must print a string of the format "Populatie(m, n, k)" as a result, where the values m , n and k must be filled out according to the current condition of the object.
5. The method `size` must print the size of the population (total amount of bacteria) as a result.
6. The method `encounter` must simulate an encounter of two bacteria, as described in the introduction. To this method, two parameters $0 \leq i, j < m+n+k$ must be given. If the bacteria i and j from the population have a different plasmid type, the plasmid of both bacteria must mutate to the third type. This is shown in the image below.



Make sure all methods are used optimally when implementing the class `Population`. The interactive

Python session below illustrates the use of the class Population.

```
>>> population = Population(m=998, n=1, k=1)
>>> print(population)
type I: 998, type II: 1, type III: 1 (after 0 encounters)
>>> print(repr(population))
Population(998, 1, 1)
>>> print(population.plasmids())
(998, 1, 1)
>>> for i in range(population.size()-1):
...     population.encounter(i, i+1)
>>> print(population)
type I: 997, type II: 0, type III: 3 (after 999 encounters)
>>> for i in range(population.size()-1):
...     population.encounter(i, i+1)
>>> print(population)
type I: 997, type II: 3, type III: 0 (after 1998 encounters)
```

Now write another function

```
simulation(population[, number][, display)
```

to which as an obligatory argument `population` an object from the class `Population` must be given. This function must simulate a given number of encounters (optional argument `number` with standard value 1), where the two bacterias that meet are always chosen randomly from the given population. To follow up on the evolution of this population throughout these encounters, the function must print both the initial condition of the population and the condition of the population every so many encounters (given by the optional argument `display` with standard value 1). The printing of the condition of the population must happen conform the format of the method `__str__` from the class `Population`. For example, the program code generates

```
population = Population(m=998, n=1, k=1)
simulation(population, 10000, 250)
```

the following output (shortened)

```
type I: 998, type II: 1, type III: 1 (after 0 encounters)
type I: 998, type II: 1, type III: 1 (after 250 encounters)
type I: 995, type II: 4, type III: 1 (after 500 encounters)
type I: 990, type II: 8, type III: 2 (after 750 encounters)
...
type I: 337, type II: 357, type III: 306 (after 9500 encounters)
type I: 328, type II: 348, type III: 324 (after 9750 encounters)
type I: 337, type II: 324, type III: 339 (after 10000 encounters)
```

Remark: Because of the non-deterministic character of the output of the function `simulation`, the accurateness of your implementation of this function will not be assessed by Pythia. In the feedback given by Pythia, however, you can verify if the evolution of the population your code generates shows the same trend as the image below.