

# Amazing Prime Sequence (hard)

This problem is a harder version of [APS](#).

Let  $f(n)$  be the smallest prime factor of  $n$ . For example,  $f(2) = 2$ ,  $f(4) = 2$  and  $f(35) = 5$ .

The sequence  $S(n)$  is defined for all positive integers as follows:

- $S(1) = 0$
- $S(n) = S(n-1) + f(n)$  (if  $n \geq 2$ )

Given  $N$ , find  $S(N)$  modulo  $2^{64}$ .

## Input

First line contains  $T$  ( $1 \leq T \leq 10000$ ), the number of test cases.

Each of the next  $T$  lines contains a single integer  $N$ . ( $1 \leq N \leq 1234567891011$ )

## Output

For each integer  $N$ , output a single line containing  $S(N)$  modulo  $2^{64}$ .

## Example

### Input

```
5
1
4
100
1000000
1000000000000
```

### Output

```
0
7
1257
37568404989
7294954823202325427
```

## Explanation for Input

-  $S(4) = 2 + 3 + 2 = 7$

-  $S(10^{12}) = 18435592284459044389811 \equiv 7294954823202325427 \pmod{2^{64}}$

## Information

There are 6 Input files.

- Input #0:  $\$1 \leq T \leq 10000$ ,  $\$1 \leq N \leq 10000$ , TL = 1s.

- Input #1:  $\$1 \leq T \leq 1000$ ,  $\$1 \leq N \leq 10^8$ , TL = 20s.

- Input #2:  $\$1 \leq T \leq 200$ ,  $\$1 \leq N \leq 10^9$ , TL = 20s.

- Input #3:  $\$1 \leq T \leq 40$ ,  $\$1 \leq N \leq 10^{10}$ , TL = 20s.

- Input #4:  $\$1 \leq T \leq 7$ ,  $\$1 \leq N \leq 10^{11}$ , TL = 20s.

- Input #5:  $\$T = 1$ ,  $\$1 \leq N \leq 1234567891011$ , TL = 20s.

My solution runs in 5.36 sec. (total time)

**Source Limit is 8 KB.**