## Counting Magical Permutatitons

## Counting Permutations

In a planet far away from Earth, there is a beautiful country named Magicland. The children of this country play a lot of interesting games with numbers. One of the most popular games is called Inversion. In this game, you will be given numbers from 1 to N . They are given in a certain order. You need to calculate all the inversions in the given permutation of the numbers. S/he who can say it first correctly wins the game. An inversion occurs when there exists a pair of indices $i$ and $j$ such that $i<j$ and given number at $i$-th position is greater than the number at $j$-th position.

For example, let us consider a permutation of numbers 1 to $5: 5,1,4,2,3$. This permutation has the following inversions: $(5,1),(5,4),(5,2),(5,3),(4,2),(4,3)$. Therefore, the number of inversion will be 6 . The first person to tell this number correctly will win this game.

For this problem, we want to know how many permutations of the numbers $1,2, \ldots, N$ will have at least $K$ inversions.
A permutation X is different from another permutation Y if there exists some $i(1<=i<=N)$ for which the number in $i$-th position is different in these two permutations.

## Input

The first line of input file contains the number of test cases, $\mathbf{T}(1<=\mathbf{T}<=50)$. Then $\mathbf{T}$ cases follow:
Each case consists of one line which contains two integers: $\mathbf{N}$ and $\mathbf{K}$.

## Constraint

For Easy version, $\mathbf{1 < =} \mathbf{N}<=\mathbf{2 0 0}$ and $0<=\mathrm{K}<=\mathbf{3 0 0}$.
For Hard version, $\mathbf{1 < =} \mathbf{N}<=\mathbf{2 0 0 0}$ and $\mathbf{0}<=\mathrm{K}<=\mathbf{3 0 0 0}$.

## Output

For each case, print "Case $\mathbf{x}$ : $\mathbf{y}$ " in a separate line, where $\mathbf{x}$ is the case number and $\mathbf{y}$ is the number of permutations with at least $K$ inversions. As the number can be very large, print y modulo 10,007.

| Sample Input | Sample Output |
| :--- | :--- |
| 3 | Case 1:5 |
| 31 | Case 2: 1 |
| 21 | Case 3: 3 |
| 32 |  |

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