# **Fast Maximum Flow**

Given a graph with N ( $2 \le N \le 5,000$ ) vertices numbered 1 to N and M ( $1 \le M \le 30,000$ ) undirected, weighted edges, compute the <u>maximum flow / minimum cut</u> from vertex 1 to vertex N.

### Input

The first line contains the two integers N and M. The next M lines each contain three integers A, B, and C, denoting that there is an edge of capacity C ( $1 \le C \le 10^9$ ) between nodes A and B ( $1 \le A$ , B  $\le$  N). Note that it is possible for there to be duplicate edges, as well as an edge from a node to itself.

## **Output**

Print a single integer (which may not fit into a 32-bit integer) denoting the maximum flow / minimum cut between 1 and N.

## **Example**

#### Input:

46

123

234

3 1 2

225

3 4 3

4 3 3

#### **Output:**

5

Viewing the problem as max-flow, we may send 3 units of flow through the path 1 - 2 - 3 - 4 and 2 units of flow through the path 1 - 3 - 4. Viewing the problem as min-cut, we may cut the first and third edges. Either way the total is 5.

Note: see also <a href="http://www.spoj.com/problems/MATCHING/">http://www.spoj.com/problems/MATCHING/</a>.