

# FOLLOWING Grado 11

Order is an important concept in mathematics and in computer science. For example, Zorn's Lemma states: "a partially ordered set in which every chain has an upper bound contains a maximal element." Order is also important in reasoning about the fix-point semantics of programs. This problem involves neither Zorn's Lemma nor fix-point semantics, but does involve order. Given a list of variable constraints of the form  $x < y$ , you are to write a program that prints all orderings of the variables that are consistent with the constraints. For example, given the constraints  $x < y$  and  $x < z$  there are two orderings of the variables  $x$ ,  $y$ , and  $z$  that are consistent with these constraints:  $xyz$  and  $xzy$ .

## Input

The input consists of a sequence of constraint specifications. A specification consists of two lines: a list of variables on one line, followed by a list of constraints on the next line.

A constraint is given by a pair of variables, where 'x y' indicates that  $x < y$ .

All variables are single character, lower-case letters. There will be at least two variables, and no more than 20 variables in a specification. There will be at least one constraint, and no more than 50 constraints in a specification. There will be at least one, and no more than 300 orderings consistent with the constraints in a specification.

Input is terminated by end-of-file.

## Output

The output should consist of the final state of the blocks world. Each original block position numbered  $i$  ( $0 \leq i < n$  where  $n$  is the number of blocks) should appear followed immediately by a colon. If there is at least a block on it, the colon must be followed by one space, followed by a list of blocks that appear stacked in that position with each block number separated from other block numbers by a space. Don't put any trailing spaces on a line. There should be one line of output for each block position (i.e.,  $n$  lines of output where  $n$  is the integer on the first line of input).

## Example

### Input:

```
10
move 9 onto 1
move 8 over 1
move 7 over 1
move 6 over 1
pile 8 over 6
pile 8 over 5
move 2 over 1
move 4 over 9
quit
```

**Output:**

0: 0

1: 1 9 2 4

2:

3: 3

4:

5: 5 8 7 6

6:

7:

8:

9: