## Pixel Shuffle



Shuffling the pixels in a bitmap image sometimes yields random looking images. However, by repeating the shuffling enough times, one finally recovers the original images. This should be no surprise, since "shuffling" means applying a one-to-one mapping (or permutation) over the cells of the image, which come in finite number.

Your program should read a number n , and a series of elementary transformations that define a "shuffling" $\phi$ of $n * n$ images. Then, your program should compute the minimal number $m(m>0)$, such that m applications of ${ }^{\phi}$ always yield the original $\mathrm{n} * \mathrm{n}$ image.

For instance if ${ }^{\phi}$ is counter-clockwise $90^{\circ}$ rotation then $\mathrm{m}=4$.


## Input

Test cases are given one after another, and a single 0 denotes the end of the input. For each test case:

Input is made of two lines, the first line is number $n\left(2<=n<=2^{10}\right.$, $n$ even). The number $n$ is the size of images, one image is represented internally by a $n$ * $n$ pixel matrix $\left(a_{i}\right)$, where $i$ is the row number and j is the column number. The pixel at the upper left corner is at row 0 and column 0 .

The second line is a non-empty list of at most 32 words, separated by spaces. Valid words are the keywords id, rot, sym, bhsym, bvsym, div and mix, or a keyword followed by -. Each keyword key designates an elementary transform (as defined by Figure 1), and key- designates the inverse of transform key. For instance, rot- is the inverse of counter-clockwise $90^{\circ}$ rotation, that is clockwise $90^{\circ}$ rotation. Finally, the list $\mathrm{k}_{1}, \mathrm{k}_{2}, \ldots, \mathrm{k}_{\mathrm{p}}$ designates the compound transform ${ }^{\phi}=$ $\mathrm{k}_{1} \mathrm{ok}_{2} \mathrm{O} \ldots \mathrm{ok}_{\mathrm{p}}$. For instance, "bvsym rot-" is the transform that first performs clockwise 900 rotation and then vertical symmetry on the lower half of the image.


Figure 1: Transformations of image $\left(a_{i j}^{j}\right)$ into image $\left(b_{i}^{j}\right)$
id, identity. Nothing changes : $b_{i}^{j}=a_{i}^{j}$.
rot, counter-clockwise $90^{\circ}$ rotation
sym , horizontal symmetry : $b_{i}^{j}=a_{i}^{n-1-j}$
bhsym, horizontal symmetry applied to the lower half of image : when $i \geq n / 2$, then $b_{i}^{j}=$ $a_{i}^{n-1-j}$. Otherwise $b_{i}^{j}=a_{i}^{j}$.
bvsym, vertical symmetry applied to the lower half of image ( $i \geq n / 2$ )
div , division. Rows $0,2, \ldots, n-2$ become rows $0,1, \ldots n / 2-1$, while rows $1,3, \ldots n-1$ become rows $n / 2, n / 2+1, \ldots n-1$.
mix , row mix. Rows $2 k$ and $2 k+1$ are interleaved. The pixels of row $2 k$ in the new image are $a_{2 k}^{0}, a_{2 k+1}^{0}, a_{2 k}^{1}, a_{2 k+1}^{1}, \cdots a_{2 k}^{n / 2-1}, a_{2 k+1}^{n / 2-1}$, while the pixels of row $2 k+1$ in the new image are $a_{2 k}^{n / 2}, a_{2 k+1}^{n / 2}, a_{2 k}^{n / 2+1}, a_{2 k+1}^{n / 2+1}, \cdots, a_{2 k}^{n-1}, a_{2 k+1}^{n-1}$.


## Output

For each test case:
Your program should output a single line whose contents is the minimal number $m(m>0)$ such that ${ }^{\phi}$ is the identity. You may assume that, for all test input, you have $\mathrm{m}<2^{31}$.

## Example

Input:
256
rot- div rot div

Output:
8
63457

