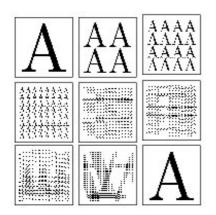
# **Pixel Shuffle**



Shuffling the pixels in a bitmap image sometimes yields random looking images. However, by repeating the shuffling enough times, one finally recovers the original images. This should be no surprise, since "shuffling" means applying a one-to-one mapping (or permutation) over the cells of the image, which come in finite number.

Your program should read a number n , and a series of elementary transformations that define a "shuffling"  $\phi$  of n \* n images. Then, your program should compute the minimal number m (m > 0) , such that m applications of  $\phi$  always yield the original n \* n image.

For instance if  $\phi$  is counter-clockwise 90° rotation then m = 4.



## Input

Test cases are given one after another, and a single 0 denotes the end of the input. For each test case:

Input is made of two lines, the first line is number n (2 <= n <=  $2^{10}$ , n even). The number n is the size of images, one image is represented internally by a n \* n pixel matrix ( $a^{j}_{i}$ ), where i is the row number and j is the column number. The pixel at the upper left corner is at row 0 and column 0.

The second line is a non-empty list of at most 32 words, separated by spaces. Valid words are the keywords **id**, **rot**, **sym**, **bhsym**, **bvsym**, **div** and **mix**, or a keyword followed by -. Each keyword **key** designates an elementary transform (as defined by Figure 1), and **key-** designates the inverse of transform **key**. For instance, **rot-** is the inverse of counter-clockwise 90° rotation, that is clockwise 90° rotation. Finally, the list  $k_1, k_2, ..., k_p$  designates the compound transform  $\phi = k_1 \circ k_2 \circ ... \circ k_p$ . For instance, "bvsym rot-" is the transform that first performs clockwise 90° rotation and then vertical symmetry on the lower half of the image.



Figure 1: Transformations of image (a<sup>j</sup><sub>i</sub>) into image (b<sup>j</sup><sub>i</sub>)

id , identity. Nothing changes :  $b_i^j = a_i^j$ .

rot , counter-clockwise  $90^{\circ}$  rotation

- $\mathbf{sym}\,$  , horizontal symmetry :  $b_i^j = a_i^{n-1-j}$
- **bhsym**, horizontal symmetry applied to the lower half of image : when  $i \ge n/2$ , then  $b_i^j = a_i^{n-1-j}$ . Otherwise  $b_i^j = a_i^j$ .
- $\mathbf{bvsym}$  , vertical symmetry applied to the lower half of image  $(i \geq n/2)$
- div , division. Rows  $0, 2, \ldots, n-2$  become rows  $0, 1, \ldots n/2 1$ , while rows  $1, 3, \ldots n-1$  become rows  $n/2, n/2 + 1, \ldots n 1$ .
- **mix**, row mix. Rows 2k and 2k+1 are interleaved. The pixels of row 2k in the new image are  $a_{2k}^0, a_{2k+1}^0, a_{2k}^1, a_{2k+1}^1, \cdots, a_{2k}^{n/2-1}, a_{2k+1}^{n/2-1}$ , while the pixels of row 2k + 1 in the new image are  $a_{2k}^{n/2}, a_{2k+1}^{n/2}, a_{2k}^{n/2+1}, a_{2k+1}^{n/2+1}, \cdots, a_{2k}^{n-1}, a_{2k+1}^{n-1}$ .

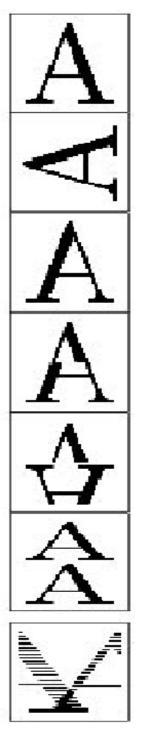
## Output

For each test case:

Your program should output a single line whose contents is the minimal number m (m > 0) such that  $\phi$  is the identity. You may assume that, for all test input, you have m <  $2^{31}$ .

#### Example

#### Input: 256 rot- div rot div



bvsym div mix 

#### Output: