# **Periodic function, trip 3**

Solar cycle predictions are used by various agencies and many industry groups. The solar cycle is important for determining the lifetime of satellites in low-Earth orbit, as the drag on the satellites correlates with the solar cycle [...]. (NOAA)

#### (Solar Cycle)

Sunspot Number Progression : Observed data through May 2008 ; Dec 2012 ; Nov 2014

The goal of the problem is to propose a perfect prediction center, with weak constraints.

Let us consider periodic functions from Z to R.

**def f(x): return [4, -6, 7][x%3]** # (with Python notations) # 4, -6, 7, 4, -6, 7, 4, -6, 7, 4, -6, 7, 4, -6, 7, ...

For example, *f* is a 3-periodic function, with f(0) = f(3) = f(6) = f(9) = 4.

With a simplified notation we will denote f as [4, -6, 7].

For two periodic functions (with integral period), the quotient of periods will be rational, in that case it can be shown that the sum of the functions is also a periodic function. Thus, the set of all such functions is a vector space over  $\mathbf{R}$ .

For that problem, we consider a function that is the sum of several periodic functions all with as period an integer N at maximum. You will be given some starting values, you'll have to find new ones.

#### Input

On the first line, you will be given an integer N.

On the second line, you will be given integers y: the first (0-indexed)  $N \times N$  values of a periodic function f that is sum of periodic functions all with as period an integer N at maximum. On the third line, you will be given  $N \times N$  integers x.

#### Output

Print f(x) for all required x. See sample for details.

#### Example

Output: 16 16 16 16 16 16 16 16 16 16

#### Explanation

For example *f* can be seen as the sum of three periodic functions : [10] + [5, -8] + [0, 1, 2] (with simplified notations ; periods are 1,2 and 3) In that case *f*(10) = [10][10%1] + [5, -8][10%2] + [0, 1, 2][10%3] = 10 + 5 + 1 = 16, and so on.

## Constraints

N < 51 abs(y) < 10^9 0 < x < 10^9

### Informations

The problem is not simple, but constraints allow easy coding with C-like languages. You can safely assume output fit in a signed 32bit container. Time limit is at least ×4 my basic C timing. It could be hard with slow languages. There's 4 input files, with increasing value of N. You may first try the easy edition <u>PERIOD4</u>. **Have fun ;-)** 

edit(09/06/2016) If it's too easy ; PERIOD5 is made for you.