

Recursive Sequence

Sequence (a_i) of natural numbers is defined as follows:

$$a_i = b_i \text{ (for } i \leq k)$$

$$a_i = c_1 a_{i-1} + c_2 a_{i-2} + \dots + c_k a_{i-k} \text{ (for } i > k)$$

where b_j and c_j are given natural numbers for $1 \leq j \leq k$. Your task is to compute a_n for given n and output it modulo 10^9 .

Input

On the first row there is the number C of test cases (equal to about 1000).

Each test contains four lines:

k - number of elements of (c) and (b) ($1 \leq k \leq 10$)

b_1, \dots, b_k - k natural numbers where $0 \leq b_j \leq 10^9$ separated by spaces

c_1, \dots, c_k - k natural numbers where $0 \leq c_j \leq 10^9$ separated by spaces

n - natural number ($1 \leq n \leq 10^9$)

Output

Exactly C lines, one for each test case: a_n modulo 10^9

Example

Input:

```
3
3
5 8 2
32 54 6
2
3
1 2 3
4 5 6
6
3
24 354 6
56 57 465
98765432
```

Output:

```
8
714
257599514
```