

Recursive Sequence (Version III)

Sequence (a_i) of natural numbers is defined as follows:

$$a_i = b_j \text{ if } i \leq k$$

$$a_i = c_1 a_{i-1} + c_2 a_{i-2} + \dots + c_k a_{i-k} \text{ if } i > k$$

where b_j and c_j are given natural numbers for $1 \leq j \leq k$. Your task is to compute $a^2_m + a^2_{m+1} + a^2_{m+2} + \dots + a^2_n$ for given $m \leq n$ and output it modulo a given positive integer p (not necessarily prime).

Input

On the first row there is the number T of test cases ($T \leq 50$).

Each following test case contains four lines:

- k - number of elements of (c) and (b) ($1 \leq k \leq 15$)
- b_1, \dots, b_k - k natural numbers where $0 \leq b_j \leq 10^9$ separated by spaces
- c_1, \dots, c_k - k natural numbers where $0 \leq c_j \leq 10^9$ separated by spaces
- m, n, p - natural numbers separated by spaces ($1 \leq m \leq n \leq 10^{18}$, $1 \leq p \leq 10^8$)

Output

Exactly T lines, one for each test case: $(a^2_m + a^2_{m+1} + a^2_{m+2} + \dots + a^2_n)$ modulo p .

Example

Input:

```
2
3
2 3 5
1 2 3
10 15 1000000
15
401 131 940 406 673 592 532 452 733 966 602 600 61 212 257
13 12 81 75 37 12 10 35 25 75 16 90 27 33 47
2 85704376 99999991
```

Output:

```
248783
32397016
```

Note

You can try the problem [SPP](#) first.