

# Transitive Closure

In mathematics, a set  $S$  is transitive if whenever an element  $a$  is related to an element  $b$ , and  $b$  is in turn related to an element  $c$ , then  $a$  is also related to  $c$ . In other words, any set of pairs is transitive if and only if you have  $(a,b)$  and  $(b,c)$  then you also must have  $(a,c)$ . Check this example:  $S = \{ (1,2),(2,3),(3,4),(2,4) \}$ . Is set  $S$  is transitive relation ? No, Because you have  $(1,2)$  and  $(2,3)$  but you don't have  $(1,3)$  If we add  $(1,3)$  will it be transitive ? ((  $S = \{ (1,2),(2,3),(3,4),(2,4),(1,3) \}$  )) No, Because you have  $(1,3)$  and  $(3,4)$  but you don't have  $(1,4)$  If we add  $(1,4)$  will it be transitive ? ((  $S = \{ (1,2),(2,3),(3,4),(2,4),(1,3),(1,4) \}$  )) Yes, Now the set  $S$  is now transitive after we added 2 pairs  $\{ (1,3),(1,4) \}$  These pairs called transitive closure (which means the minimal pairs that convert set  $S$  into a transitive set ). Your task is given the set  $S$  you have to output the minimal pairs have to be added to make the set  $S$  transitive.

## Input

The first line of input is the number of test cases  $T$  where  $(0 < T \leq 100)$ , Each test case you'll be given the number of pairs in the set  $N$  where  $(0 < N \leq 100)$ , followed by  $N$  pairs  $(a, b)$  where  $(0 \leq a, b < N)$ .

## Output

For each test case print "Case\_#i: \_X" where "i" is the case number, "X" is the minimal number of pairs have to be added to make the set transitive and " \_ " is a white space. Each test case should be in a separate line.

## Example

### Input:

```
3
4
0 1
1 2
2 3
1 3
2
0 1
1 0
1
0 0
```

### Output:

```
Case #1: 2
Case #2: 2
Case #3: 0
```